

**DOCTORAL (PHD) STUDIES  
COURSE DESCRIPTION**

Course title	Field of science	Faculty	Institute
<b>Functional Analysis</b>	Mathematics (N 001)	Faculty of Mathematics and Informatics	Institute of Applied Mathematics
Study method	Number of credits	Study method	Number of credits
Lectures	2	Consultations	1
Individual work	7	Seminars	0

**Course summary**

1. **Sets and relations.** Basic concepts and axioms.
2. **Metric spaces.** Sets of metric spaces. Complete metric spaces. Contraction mapping. Baire category theorem. Separable spaces.
3. **Topological spaces.** Bases. Nets. Continuous functions. Compact spaces. Topological vector spaces.
4. **Compactness in metric spaces.**
5. **Linear spaces.** Convex sets and functionals. Hahn–Banach theorem.
6. **Normed vector spaces and their geometric properties.** Banach spaces. Spaces with Schauder basis.
7. **Inner product spaces.** Hilbert spaces. Fourier series.
8. **Linear functionals.** Dual continuous space. Weak topologies. Distributions.
9. **Continuous linear operators.** Uniform boundedness principle. Closed graph theorem. Inverse, regular and adjoint operators. Compact operators.
10. **Elements of spectral theory.** Spectrum and resolvent. Spectrum of self-adjoint operators..
11. **Linear equations.** Fredholm – Riesz – Schauder theory.
12. **Differential calculus.** Fréchet, Gateaux derivatives. Higher order derivatives, Taylor formula. Newton's method.
13. **Nonlinear equations.** Schauder principle. Fixed point theorems.

**Total number of contact hours: 64 academic hours.**

**Main literature**

1. V. Paulauskas, A. Račkauskas. *Funkcinė analizė*. I knyga. Erdvės; II knyga. Funkcijos ir lygtys. 2007, Vilnius.
2. A.N. Kolmogorov, S.V. Fomin. *Introductory Real Analysis*. Dover, New York, 1970
3. G. K Pedersen. *Analysis Now*. 1988, Springer, New York.
4. D.H. Griffel. *Applied Functional Analysis*. 1981, Wiley, New York.

Consulting teacher	Scientific degree	Pedagogical name	Main publications in the field of science of the last 5 year period
Artūras Štikonas	Dr. (HP)	Prof.	<ol style="list-style-type: none"> <li>1. K. Bingelė, A. Bankauskienė, A. Štikonas. Spectrum curves for a discrete Sturm–Liouville problem with one integral boundary condition. <i>Nonlinear Anal. Model. Control</i>, 24(5):755–774, 2019. <a href="https://doi.org/10.15388/NA.2019.5.5">https://doi.org/10.15388/NA.2019.5.5</a></li> <li>2. M. Sapagovas, J. Novickij, A. Štikonas. Stability analysis of a weighted difference scheme for two-dimensional hyperbolic equations with integral conditions. <i>Electron. J. Differential Equations</i>, 2019(04):1–13, 2019. <a href="https://ejde.math.txstate.edu/Volumes/2019/04/abstr.html">https://ejde.math.txstate.edu/Volumes/2019/04/abstr.html</a></li> <li>3. K. Bingelė, A. Bankauskienė, A. Štikonas. Investigation of spectrum curves for a Sturm–Liouville problem with two-point nonlocal boundary conditions. <i>Math. Model. Anal.</i>, 25(1):53–70, 2020. <a href="https://doi.org/10.3846/mma.2020.10787">https://doi.org/10.3846/mma.2020.10787</a></li> </ol>

			<p>4. E. Şen, A. Štikonas. Asymptotic distribution of eigenvalues and eigenfunctions of a nonlocal boundary value problem. <i>Math. Model. Anal.</i>, 26(2):253–266, 2021. <a href="https://doi.org/10.3846/mma.2021.13056">https://doi.org/10.3846/mma.2021.13056</a></p> <p>5. A. Štikonas, E. Şen. Asymptotic analysis of Sturm–Liouville problem with nonlocal integral-type boundary condition. <i>Nonlinear Anal. Model. Control</i>, 26(5):969–991, 2021. <a href="https://doi.org/10.15388/namc.2021.26.24299">https://doi.org/10.15388/namc.2021.26.24299</a></p>
Alfredas Račkauskas	Habil. dr.	Prof.	<p>1. A. Račkauskas. Asymptotic normality of sums of Hilbert space valued random elements. <i>Georgian mathematical journal</i>. 28(3):459–469, 2021. <a href="https://doi.org/10.1515/gmj-2019-2075">https://doi.org/10.1515/gmj-2019-2075</a></p> <p>2. R. Norvaiša, A. Račkauskas. Uniform asymptotic normality of weighted sums of short-memory linear processes. <i>Journal of applied probability</i>, 57(1):174–195, 2020. <a href="https://doi.org/10.1017/jpr.2019.86">https://doi.org/10.1017/jpr.2019.86</a></p> <p>3. A. Račkauskas, M. Wendler. Convergence of U-processes in Holder spaces with application to robust detection of a changed segment. <i>Statistical papers</i>, 61(4):1409–1435 <a href="https://doi.org/10.1007/s00362-020-01161-9">https://doi.org/10.1007/s00362-020-01161-9</a></p> <p>4. A. Račkauskas, Ch. Suquet. On Bernstein-Kantorovich invariance principle in Holder spaces and weighted scan statistics, <i>ESAIM: probability and statistics</i>, 24:186–206, 2020. <a href="https://doi.org/10.1051/ps/2019027">https://doi.org/10.1051/ps/2019027</a></p> <p>5. R. Norvaiša, A. Račkauskas. Uniform asymptotic normality of self-normalized weighted sums of random variables <i>Lithuanian mathematical journal</i>, 59(4): 575–594, 2019 <a href="https://doi.org/10.1007/s10986-019-09461-w">https://doi.org/10.1007/s10986-019-09461-w</a></p>

Approved by the Board of Faculty of Mathematics and Informatics 10/12/2021. Resolution No. (1.5 E) 110000-TPN-42

Board Chairman – assoc. prof. dr. Kristina Lapin