Course description

| Course title | Course code |
| :--- | :--- |
| Time series analysis |  |


| Lecturer | Department where the course is delivered |
| :--- | :--- |
| Prof. Remigijus Leipus | Department of Statistical Analysis <br>  <br>  <br>  <br>  <br>  <br>  <br>  <br>  <br>  <br> Fastitute of Applied Mathematics <br> Naugarduko St. 24, LT-03225 Vilnius, Lithuania |


| Cycle |  | Type of course |
| :--- | :--- | :--- |
| Second |  | Compulsory |


| Mode of delivery | Semester or period when the course is delivered | Language of <br> instruction |
| :--- | :--- | :--- |
| Face-to-face | $1^{\text {st }}$ semester (Fall) | Lithuanian, English |


|  | Prerequisites and corequisites |
| :--- | :--- |
| Prerequisites: | Corequisites (if any): |
| Mathematical statistics, Probability theory |  |


| Number of <br> ECTS credits | Student's workload | Contact hours | Individual work hours |
| :---: | :---: | :---: | :---: |
| 5 | 125 | 40 | 85 |

## Course objectives: programme competences to be developed

The course provides advanced time series methods and models, their applications, modeling, forecasting of a real world (financial) data.

| Learning outcomes <br> At the end of the course a student <br> should: | Learning methods | Assessment <br> methods |
| :--- | :--- | :--- |
| - Know advanced time series models; <br> - Operate with the main concepts and <br> methods of the time series theory. | Lectures covering time series theory. <br> Seminars for time series problem solving, analysis of specific <br> questions or used case analysis. <br> Individual work for additional problem solving and <br> confirmation of theoretical knowledge. | Tests, <br> midterm and <br> final exam. |
| - Be able to identify, state, and solve <br> applied problems in economics, finance, <br> and other fields using time series methods; <br> - Be able to select appropriate time series <br> model. | Lectures covering applications of time series, employing used <br> case analysis. <br> Practical training for encouraging students state problems <br> and find strategies for solutions. | Tests, <br> practical <br> tasks <br> midterm and <br> final exam. |
| - Be able to use time series literature and <br> deepen theoretical knowledge. | Individual work for recommended reading. | Midterm and <br> final exam. |


|  | Contact hours |  |  |  |  | Individual work hours and assignments |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Course content: breakdown of the course |  | $\begin{aligned} & 0 \\ & \text {.0 } \\ & \frac{0}{3} \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ |  |  | n 0 0 0 0 0 0 0 0 0 0 | Individual work hours | Assignments |
| 1. Estimation and elimination of time series trend and seasonal component. | 3 |  | 2 |  | 5 | 6 | Individual study of recommended readings and solving appointed exercises |
| 2. Stochastic processes. Stationary time series. Autocovariance function. Spectral analysis. | 3 |  | 2 |  | 5 | 6 | Individual study of recommended readings and solving appointed exercises |
| 3. Long memory time series | 2 |  | 1 |  | 3 | 4 | Individual study of recommended readings and solving appointed exercises |
| 4. Autoregressive moving average time series models (ARMA). Nonstationary ARIMA, SARIMA models. | 4 |  | 3 |  | 7 | 8 | Individual study of recommended readings and solving appointed exercises |
| 5. Stylized facts of financial time series. | 2 |  | 1 |  | 3 | 5 | Individual study of recommended readings and solving appointed exercises |
| 6. Models of conditional heteroskedasticity. ARCH and GARCH models. Volatility. | 4 |  | 3 |  | 7 | 9 | Individual study of recommended readings and solving appointed exercises |
| 7. Parameter estimation of ARMA and GARCH models. | 3 |  | 2 |  | 5 | 6 | Individual study of recommended readings and solving appointed exercises |
| 8. Tests |  |  | 1 |  | 1 | 7 | Prepare for the tests |
| 9. Midterm exam | 2 |  |  |  | 2 | 17 | Recall theory and problem solving |
| 10. Final exam | 2 |  |  |  | 2 | 17 | Recall theory and problem solving |
| Total | 25 |  | 15 |  | 40 | 85 |  |


| Assessment strategy | Weight | Time of assessment | Criteria |
| :---: | :---: | :---: | :---: |
| 4 tests: <br> 20-30 min written test (each=10\%). First includes problems from topic 1 ; second topic 2, third topics 3-4, fourth topics 5-7. <br> Solutions are given points. | 40\% | During seminars, when corresponding theoretical and practical part is finished | Mark 10 - student got no less than $90 \%$ points Mark 9 - student got no less than $80 \%$ points Mark 8 - student got no less than $70 \%$ points Mark 7 - student got no less than $60 \%$ points Mark 6 - student got no less than $50 \%$ points Mark 5 - student got no less than $40 \%$ points Mark 1-4 - student got less than $40 \%$ points |


| Midterm exam: <br> 2-hour written exam, consisting of theoretical problems and exercises from topics 1-4. Solutions are given points. | 30\% | During lectures, when corresponding theoretical and practical part is finished | Mark 10 - student has perfectly mastered the material, is able to analyze and generalize it. Understands and suitably uses concepts, knows main results of time series. Has gathered not less than $90 \%$ of points. <br> Mark 8-9 - student has mastered the material very well, is able to systemize and generalize it. Understands and suitably uses concepts, knows majority of the main results of time series. Has gathered not less than $80 \%$ (mark 9); $70 \%$ (mark 8) of points. <br> Mark 6-7 - student understands major time series concepts, knows main results of time series. Has gathered not less than $60 \%$ (mark 7); $50 \%$ (mark 6) of points. <br> Mark 5 - students understanding of time series concepts is superficial, she knows some results of time series. Has gathered not less than $40 \%$ of points. <br> Mark 1-4 - student does not know the material. The usage of terms and concepts is unsuitable. Has gathered less than $40 \%$ of points. |
| :---: | :---: | :---: | :---: |
| Final exam: <br> 2-hour written exam, consisting of theoretical problems and exercises from topics 5-7. <br> Solutions are given points. | 30\% | During exam session | Mark 10 - student has perfectly mastered the material, is able to analyze and generalize it. Understands and suitably uses concepts, knows main results of time series. Has gathered not less than $90 \%$ of points. <br> Mark 8-9 - student has mastered the material very well, is able to systemize and generalize it. Understands and suitably uses concepts, knows majority of the main results of time series. Has gathered not less than $80 \%$ (mark 9); $70 \%$ (mark 8) of points. <br> Mark 6-7 - student understands major time series concepts, knows main results of time series. Has gathered not less than $60 \%$ (mark 7); $50 \%$ (mark 6) of points. <br> Mark 5 - students understanding of time series concepts is superficial, she knows some results of time series. Has gathered not less than $40 \%$ of points. <br> Mark 1-4 - student does not know the material. The usage of terms and concepts is unsuitable. Has gathered less than $40 \%$ of points. |


| Author | Publication <br> year | Title | Volume <br> and/or <br> publicati <br> on <br> number | Publication <br> place <br> publisher |
| :--- | :--- | :--- | :--- | :--- |
| and |  |  |  |  |$|$|  |
| :--- |
| Required reading |
| P.J. Brockwell, <br> R. A. Davis |
| P.J. Brockwell, <br> R. A. Davis |


| R. S. Tsay | 2010 | Analysis of Financial Time Series | $3^{\text {rd }}$ ed. | New York: <br> Wiley. |
| :--- | :--- | :--- | :--- | :--- |
| Additional reading | 1994 | Time Series Analysis | Princeton, <br> Princeton <br> University Press. |  |
| J.D. Hamilton | 2010 | Time Series: Applications to Finance with R and S- <br> Plus | $2^{\text {nd }}$ ed. | N.Y. Wiley. |
| Chan N.H. |  |  |  |  |

